

# Estimating variance components in models with additivity

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## Abstract

We compare triple minimization with a method based on the algebraic structure of the model for the estimation of variance components. To do this we consider a model in which three factors cross. The first factor has fixed effects and is additive to the other two.

## Keywords

Linear mixed models, Variance components, Maximum likelihood estimation methods, Pivot variables.

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