Improved bounds for Estrada index of graphs

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Abstract

Let G be a graph with n vertices and let $\lambda_1, \lambda_2, \ldots, \lambda_n$ be its eigenvalues. The Estrada index of G is defined in [3] as

$$EE = EE\left(G\right) = \sum_{i=1}^{n} e^{\lambda_i}.$$

In this talk, we consider the simple connected graphs with $n \geq 4$ vertices but not complete and obtain improved bounds for Estrada index of these graphs.

Keywords

Estrada index, Eigenvalue (of graph), Bound.

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